1. Prove that if G is finite and has a p-subgroup, then

$$[N_G(H) : H] \equiv [G : H] \bmod p.$$

2. Prove that if H is a p-subgroup of a finite group G such that p divides $[G : H]$, then $N_G(H) \neq H$.