

1. Let  $R$  be a set of actions, where  $a \times b$  means “first do  $b$ , then do  $a$ ” and “ $a + b$  means “choose between doing  $a$  and  $b$ . In the literature, this is called either a “process algebra” or an “action algebra.”
  - (a) Give an example to show that distributivity fails.
  - (b) What is the multiplicative identity element?
  - (c) Is there an additive identity element? If so, what is it? If not, why not.
2. Show that the set of continuous functions from the reals to the reals is a ring, where  $+$  is pointwise addition and  $\times$  is composition.