

5. No, the leftmost 1 in the second row is not to the right of the leftmost 1 in the first row.      6. Yes.

7. Yes.

9. There are infinitely many solutions represented by the system

$$\begin{cases} x = 2z + 6 \\ y = -3z + 1 \end{cases}$$

where  $z$  is the parameter, can be assigned any value, and used to compute values of  $x$  and  $y$ .

11. The system has one solution. It is  $x = -1$ ,  $y = 3$ , and  $z = 4$  or, written as an ordered triple,  $(-1, 3, 4)$ .

17. Write the system as the augmented matrix,  $\left[ \begin{array}{cc|c} 3 & -3 & 12 \\ 3 & 2 & -3 \\ 2 & 1 & 4 \end{array} \right]$ .

Then use row operations to find the reduced row-echelon form.

$$\begin{aligned} & \left[ \begin{array}{cc|c} 3 & -3 & 12 \\ 3 & 2 & -3 \\ 2 & 1 & 4 \end{array} \right] \xrightarrow{R_1 = \frac{1}{3}r_1} \left[ \begin{array}{cc|c} 1 & -1 & 4 \\ 3 & 2 & -3 \\ 2 & 1 & 4 \end{array} \right] \xrightarrow{\substack{R_2 = -3r_1 + r_2 \\ R_3 = -2r_1 + r_3}} \left[ \begin{array}{cc|c} 1 & -1 & 4 \\ 0 & 5 & -15 \\ 0 & 3 & -4 \end{array} \right] \\ & \xrightarrow{R_2 = \frac{1}{5}r_2} \left[ \begin{array}{cc|c} 1 & -1 & 4 \\ 0 & 1 & -3 \\ 0 & 3 & -4 \end{array} \right] \xrightarrow{\substack{R_1 = r_2 + r_1 \\ R_3 = -3r_2 + r_3}} \left[ \begin{array}{cc|c} 1 & 0 & 1 \\ 0 & 1 & -3 \\ 0 & 0 & 5 \end{array} \right] \xrightarrow{R_3 = \frac{1}{5}r_3} \left[ \begin{array}{cc|c} 1 & 0 & 1 \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{array} \right] \end{aligned}$$

There is no solution. The system is inconsistent.

19. Write the system as the augmented matrix, 
$$\left[ \begin{array}{cc|c} 2 & -4 & 8 \\ 1 & -2 & 4 \\ -1 & 2 & -4 \end{array} \right].$$

Then use row operations to find the reduced row-echelon form.

$$\left[ \begin{array}{cc|c} 2 & -4 & 8 \\ 1 & -2 & 4 \\ -1 & 2 & -4 \end{array} \right] \xrightarrow{\substack{\text{Interchange} \\ \text{rows 1 and 2}}} \left[ \begin{array}{cc|c} 1 & -2 & 4 \\ 2 & -4 & 8 \\ -1 & 2 & -4 \end{array} \right] \xrightarrow{\substack{R_2 = -2r_1 + r_2 \\ R_3 = r_1 + r_3}} \left[ \begin{array}{cc|c} 1 & -2 & 4 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right]$$

The system has an infinite number of solutions. They are  $x = 2y + 4$ , where  $y$  is the parameter and can be assigned any real number.

23. Write the system as the augmented matrix, 
$$\left[ \begin{array}{cccc|c} 1 & 1 & 0 & 0 & 7 \\ 0 & 1 & -1 & 1 & 5 \\ 1 & -1 & 1 & 1 & 6 \\ 0 & 1 & 0 & -1 & 10 \end{array} \right].$$

Then use row operations to find the reduced row-echelon form.

$$\left[ \begin{array}{cccc|c} 1 & 1 & 0 & 0 & 7 \\ 0 & 1 & -1 & 1 & 5 \\ 1 & -1 & 1 & 1 & 6 \\ 0 & 1 & 0 & -1 & 10 \end{array} \right] \xrightarrow{R_3 = -r_1 + r_3} \left[ \begin{array}{cccc|c} 1 & 1 & 0 & 0 & 7 \\ 0 & 1 & -1 & 1 & 5 \\ 0 & -2 & 1 & 1 & -1 \\ 0 & 1 & 0 & -1 & 10 \end{array} \right] \xrightarrow{\substack{R_1 = -r_2 + r_1 \\ R_3 = 2r_2 + r_3 \\ R_4 = -r_2 + r_4}} \left[ \begin{array}{cccc|c} 1 & 0 & 1 & -1 & 2 \\ 0 & 1 & -1 & 1 & 5 \\ 0 & 0 & -1 & 3 & 9 \\ 0 & 0 & 1 & -2 & 5 \end{array} \right]$$

$$\xrightarrow{R_3 = -r_3} \left[ \begin{array}{cccc|c} 1 & 0 & 1 & -1 & 2 \\ 0 & 1 & -1 & 1 & 5 \\ 0 & 0 & 1 & -3 & -9 \\ 0 & 0 & 1 & -2 & 5 \end{array} \right] \xrightarrow{\substack{R_1 = -r_3 + r_1 \\ R_2 = r_3 + r_2 \\ R_4 = -r_3 + r_4}} \left[ \begin{array}{cccc|c} 1 & 0 & 0 & 2 & 11 \\ 0 & 1 & 0 & -2 & -4 \\ 0 & 0 & 1 & -3 & -9 \\ 0 & 0 & 0 & 1 & 14 \end{array} \right] \xrightarrow{\substack{R_1 = -2r_4 + r_1 \\ R_2 = 2r_4 + r_2 \\ R_3 = 3r_4 + r_3}} \left[ \begin{array}{cccc|c} 1 & 0 & 0 & 0 & -17 \\ 0 & 1 & 0 & 0 & 24 \\ 0 & 0 & 1 & 0 & 33 \\ 0 & 0 & 0 & 1 & 14 \end{array} \right]$$

There is one solution,  $x_1 = -17$ ,  $x_2 = 24$ ,  $x_3 = 33$ , and  $x_4 = 14$  or  $(-17, 24, 33, 14)$ .